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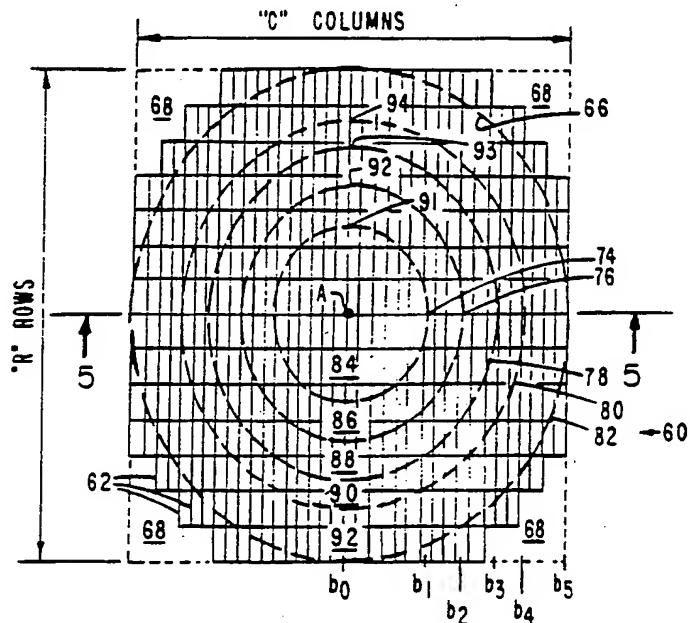
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(54) Title: LOW SIDELOBE SOLID STATE ARRAY ANTENNA APPARATUS AND PROCESS FOR CONFIGURING AN ARRAY ANTENNA APERTURE

(57) Abstract

A low sidelobe, solid state array antenna apparatus comprises a large radiating aperture divided into a large number, N, of small, closely spaced radiating apertures, each small radiating aperture having associated therewith a radiating element and a linearly polarized solid state power module. The large radiating aperture is divided into M, preferably between (3) and about (10), differently sized, elliptically shaped, concentric radiating zones superimposed, for analysis purposes, upon another. Each such zone has an output voltage amplitude,  $E_i$ , and semi-major and semi-minor axes of respective lengths,  $a_i$  and  $b_i$ , each zone being considered separately in the far field equation:  $G(\theta, \Phi) = [f(\theta, \Phi) (\hat{a}_\theta \cos \Phi - \hat{a}_\Phi \sin \Phi \cos \theta)]^2$ , wherein  $f(\theta, \Phi) = (I_i, u_i = (II_i, J_1(u_i))$  is the first order Bessel function,  $\hat{a}_\theta$  and  $\hat{a}_\Phi$  are unit vectors in the spherical coordinates and  $K_0$  is the wave number associated with the radiated field. Using the far field equation, values of  $E_i$ ,  $a_i$  and  $b_i$  for each zone are computed which result in the far field sidelobe peak gain being a minimum or being a specified number of dB, for example, at least about 30 dB, below the far field mainlobe gain. The values of  $E_i$  in overlapping zones are summed to establish the required voltage amplitudes of the underlying power modules associated with the N radiation apertures.



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LOW SIDELOBE SOLID STATE ARRAY ANTENNA APPARATUS AND  
PROCESS FOR CONFIGURING AN ARRAY ANTENNA APERTURE

1

BACKGROUND OF THE INVENTION

1. Field of the Invention

5        The present invention relates generally to the field of solid state, active aperture array antennas for radar, and more particularly to apparatus and methods for reducing sidelobe radiation by such antennas.

2. Discussion of the Background

10       Radar antennas are well known to radiate microwave radiation in a broad pattern which, for directed antenna, includes a narrow mainlobe and wide sidelobes of radiation. By common definition, the mainlobe is the central lobe of a directional antenna's radiation pattern, the sidelobes referring to the lesser lobes of progressively decreasing amplitude on both sides of the mainlobe and often extending rearwardly of the mainlobe.

15       Radar antenna aperture configuration generally determines the extent and relative magnitude of the associated sidelobes; however, the gain of the strongest one of the sidelobes is typically only about 1/64 that of the mainlobe. In terms of decibels, the strongest sidelobe gain is typically down about 18dB from the associated mainlobe gain. Gains of the other sidelobes

1 are usually considerably smaller than that of the  
strongest sidelobe. Although sidelobe gain is typically  
much smaller than mainlobe gain, because of the large  
solid angle into which sidelobes radiate, as compared to  
5 the small solid angle into which the mainlobe radiates,  
typically about 25 percent of the total power radiated  
by a uniformly illuminated radar antenna in the sidelobes.

Ordinarily, sidelobe radiation provides no useful  
function and in addition to representing wasted radiating  
10 power has other serious disadvantages. For example,  
radar clutter from sidelobe returns increases the  
difficulty of discriminating targets from background.  
Another very significant disadvantage of sidelobe  
radiation is that such radiation can, in a military  
15 environment, be utilized by hostile forces for electronically  
jamming the radar and can also be used for positionally  
locating and for guiding munitions to the radar. In this  
regard, although mainlobe radiation is ordinarily much  
greater than sidelobe radiation, its relatively small  
20 solid angle of radiation and its directionality makes  
mainlobe jamming, radar location and munitions direction  
more difficult.

For these and other reasons, the reduction or  
suppression of radar sidelobe radiation is, particularly  
25 in military radar, important and military procurement  
documents establishing rigid limits on sidelobe radiation  
are not uncommon.

It is generally known that sidelobe radiation can  
be suppressed in array-type radar antennas by "tapering"  
30 the illumination over the aperture so that individual  
radiation-emitting elements near the side edges of the  
array radiate less energy than other elements closer to  
the center of the array. Power may, for example, be  
individually applied to emitting elements of the array,  
35 so that the radiation energy distribution across the  
array, in at least one direction, is substantially Gaussian.

1 Radar arrays have, until quite recently, been  
"passive" types in which each radiating element in the  
array is provided power from a large, common power  
source. For such passive arrays, tapering of the  
5 radiation output, or, as it is sometimes termed, tapering  
of array illumination, is comparatively easy to implement  
by the use of restrictive branching from the power  
source to the radiating elements, such that progressively  
lower power is provided to elements further from the  
10 array center.

More recently, however, there has been great  
interest in developing active aperture arrays in which  
each radiating element, or a subgroup of elements, in the  
array is driven by a separate, small, solid state power  
15 supply or module. Active arrays have numerous actual  
and potential advantages over passive arrays. As an  
example, the power modules of the active arrays, being  
physically dispersed across the array, can be cooled  
more efficiently and effectively than the single, high  
20 power source of a corresponding passive array. Moreover,  
within a large active array, a comparative large number  
of power modules can fail or malfunction without  
substantially impairing effectiveness of the antenna.  
In contrast, failure or malfunction of the common power  
25 source in a passive array incapacitates the entire  
antenna.

According to theory, the providing of very smoothly  
tapered illumination of passive array antennas should  
be possibly by the use of many (about 20 or more) different  
30 groups of power modules, each group having a different  
power output. In reality, however, the use of many  
different power groups of modules is not practical  
because such construction adds substantially to the cost  
of producing the arrays and causes subsequent maintenance

1 and logistical support problems. As an illustration,  
if twenty different power modules groups were to be  
used in an array, supplies of all twenty different  
type modules would have to be stocked wherever any  
5 array maintenance and repair activities are expected to  
be needed.

As a result of costs and problems involved with  
using a large number of different power module groups in  
active arrays, sidelobe reduction has generally been  
10 attempted using only a relatively few different power  
module groups which have heretofore provided only  
coarsely tapered array illumination and relatively poor  
side lobe reduction. The selection of power module  
operating levels and arrangement has, so far as is  
15 known to the present inventors, been previously made  
merely by approximately fitting the resulting,  
staircase-shaped distribution, having only a few steps,  
to an optimal distribution which may, for example, be  
in the bell-shape of a Gaussian distribution. Such  
20 fitting of an actual, stepped distribution to an optimum  
distribution curve has not heretofar, also so far as is  
known to the present inventors, been based upon any  
rigorous, systematic analysis and has not, therefore,  
except possibly in isolated, accidental cases, resulted  
25 in minimal sidelobes. Nor have such heretofore used  
curve-fitting approaches enabled specific sidelobe  
radiation levels to be predicted or designed to, as is  
often required to meet procurement specifications.

1           As a result, to satisfy present and anticipated,  
future low sidelobe requirements for solid state active  
array antennas, improvements are required in the design  
of such antennas, and specifically in processes for the  
5    systematic selection of power module operating levels  
and physical arrangements of power modules operating at  
different power levels so as to provide low sidelobes.  
It is to such a systematic approach for power  
module operating levels and arrangements that the  
10   present invention is directed.

SUMMARY OF THE INVENTION

According to the present invention, a low sidelobe  
solid state, phased array antenna apparatus, having a far  
15   field mainlobe and sidelobe radiation pattern, comprises  
an antenna aperture formed of a large number,  $N$ , of  
small, closely spaced radiating apertures;  $N$  small,  
linearly polarized radiating elements, each operatively  
associated with a corresponding small radiating aperture  
20   for radiating microwave energy therethrough; and a  
number, preferably equal to the number,  $N$ , of solid  
state power modules, each operatively associated with  
at least one corresponding radiating element for providing  
power thereto. The power modules are divided into a  
25   number,  $M$ , of specifically arranged groups of modules,  
the number  $M$  preferably being between 3 and about 10,  
being more preferably between 3 and about 7 and being  
most preferably equal to about 5. The output voltage  
30   amplitude of each of the power modules is the same in  
any group of modules, but is substantially different  
in different groups of modules. The voltages amplitudes  
of the power modules for the different module groups  
and the boundaries of the  $M$  groups of modules are  
selected so as to cause the far field sidelobe peak  
35   gain to be down at least about 30dB from the associated  
far field mainlobe gain of the array.

1        According to an embodiment, the M groups of power  
modules are concentrically arranged around a central  
point of the array so that the voltage amplitudes of  
the power modules in the groups of modules decrease  
5        with increasing distance from the array central point.  
Also, according to an embodiment, the outer boundary of  
each group of modules is elliptically shaped, having  
respective semi-major and semi-minor axes  $a_i$  and  $b_i$ .  
It should be pointed out that a circular boundary is  
10      just a special case of this analysis wherein the aspect  
ratio  $a_i/b_i$  is equal to one. Also, without loss of  
generality, the shape of each elliptical boundary can be  
chosen to have the same aspect ratio for convenience of  
design. The output voltage amplitudes and the arrangement  
15      of the groups of power modules are selected by treating  
the module groups as being formed of, or comprising, a  
superposition of M overlapping, elliptically-shaped  
zones, each such zone having the same boundary as a  
corresponding one of the module groups. Each of the M  
20      zones has associated therewith a voltage amplitude,  $E_i$ .  
The voltage amplitude of the power modules in each  
group of modules is determined by treating the M module  
voltage amplitudes as a superposition of the voltage  
amplitudes,  $E_i$ , of the corresponding overlapped  
25      zones. In conjunction therewith, the zone voltage  
amplitudes,  $E_i$ , and the group boundary semi-major and  
semi-minor axes,  $a_i$  and  $b_i$ , respectively, are selected  
by application of the following expression for the far  
field.

30        
$$G(0, \phi) = [f(0, \phi) (\hat{a}_0 \cos \phi - \hat{a}_\phi \sin \phi \cos 0)]^2,$$

wherein 
$$f(0, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i,$$

35        
$$u_i = (k_0 a_i \sin 0) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

1            $J_1^{(u_i)}$  is the first order Bessel function,  
5            $\hat{a}_0$  and  $\hat{a}_\phi$  are the unit vectors in the spherical  
10          coordinate system and  $k_0$  is the wave number equal to  
15           $2\pi/\lambda$ , with  $\lambda$  being the wavelength associated with  
20          the radiated field.

A corresponding process is provided for configuring low sidelobe array antennas, the process comprising forming an array antenna aperture from a large number,  $N$ , of small radiating apertures, providing for each radiating aperture a radiating element and a power module for supplying power to the radiating element, dividing the power modules into  $M$  different output voltage level groups and selecting the configuration of the groups of power modules and the output voltages amplitudes thereof so as to cause the far field sidelobe gain to be down at least about 30dB from the corresponding far field mainlobe gain.

The process includes treating the arrangement of the  $M$  groups of modules as a superposition of  $M$  overlapping, elliptical radiating zones having the same boundaries as the power module groups, the output voltages amplitude for any group of modules being equal to the sum of the voltage amplitudes,  $E_i$ , of the superimposed radiating zones, the semi-major and semi-minor axes  $a_i$  and  $b_i$  of the zones and the voltage amplitude levels  $E_i$  thereof being selected in accordance with the above equation to provide a far field sidelobe gain which is at least about 30dB down from the associated far field mainlobe gain.

30           BRIEF DESCRIPTION OF THE DRAWINGS

A better understanding of the present invention may be had by considering the accompanying drawings in which:

35          FIG. 1 is an exploded perspective of an exemplary solid state, active array antenna with which the present invention may be used to advantage;

1           FIG. 2 is a pictorial drawing of the radiation  
pattern of a typical airborne radar, showing mainlobe  
and sidelobe portions of the radiation pattern;

5           FIG. 3 is a diagram depicting the coordinate  
system used to specify the coordinatee of the far field  
relative to an radiating antenna;

10          FIG. 4 is a diagram depicting the manner in  
which a generally rectangular solid state active array  
antenna is divided into a series of M concentric, over-  
lapping elliptical power module zones, each such zone  
having a different power level;

15          FIG. 5 is a diagram showing, relative to an  
array cross-section taken generally along line 5-5 of  
FIG. 4, how the aperature illumination taper is provided  
by superimposing different voltage levels of power  
modules in the different module zones of FIG. 4;

20          FIG. 6 is a diagram, similar to right hand  
portions of the diagram of FIG. 5, showing, for a  
particular array configuration and sidelobe radiation  
requirement, normalized power levels for five power  
module zones, the corresponding, normalized zone boundary  
dimensions being also indicated;

25          FIG. 7 is a graph plotting far field mainlobe  
and sidelobe gain vs angle from broadside axis for the  
conditions shown in FIG. 6; idealized, elliptical  
aperture zones being assumed; and

30          FIG. 8 is a graph plotting far field mainlobe and  
sidelobe gain vs angle from broadside axis for conditions  
in which stepped zone boundaries corresponding to  
actual module lattice configuration are assumed.

1                    DESCRIPTION OF THE PREFERRED EMBODIMENT

There is shown in FIG. 1, in exploded form, an exemplary, solid state, active array antenna 10 of the general type with which the present invention may be used to advantage. Comprising antenna 10, which is shown as an aircraft-mounted type, are an aperture assembly 12, a cooling liquid plate assembly 14, a solid state power module assembly 16 and a stripline feed assembly 18. Included in aperture assembly 12 is a large number of small radiating elements 24, each of which has disposed therein a dielectric filler 26. Defined in a face 28 of aperture assembly 12 is a large number of openings 30, each of such openings being associated with one of radiating elements 24. Mounted on cooling plate assembly 14 are a number of loop assemblies 32, each of which is also associated with one of radiating elements 24. A large number of solid state power modules 34 comprise power module assembly 16, each such module preferably, but not necessarily, powering only a single associated radiating element 24.

The present invention is principally directed towards providing preselected voltage operating levels of power modules (corresponding to modules 34) and the physical arrangement of such modules in an assembly (corresponding to module assembly 16) so that the far field radiation from the antenna exhibits very low sidelobes. With respect to sidelobes, FIG. 2 illustrates a typical radiation pattern 38 associated with a radar carried by an aircraft 40. The airborne radar involved may, for example, comprise a solid state active array similar to array 10 depicted in FIG. 1. As shown in FIG. 2, radiation pattern 38 comprises a narrow, beam-shaped mainlobe 42 and smaller, fan-shaped sidelobes 44 on each side of the mainlobe. Sidelobes 44 comprise several different lobes 46 which fan out at different angles,  $\alpha$ , relative to a main beam axis 48; typically

1 the sidelobes diminish in intensity as the angle,  $\alpha$  increases. It can further be seen from FIG. 2 that some of lobes 46 extend rearwardly relative to mainlobe 42, the angles,  $\alpha$ , associated therewith being greater  
5 than 90°.

As more particularly described below, the present invention relates to a process for configuring a solid state, active array so that the far field sidelobe gain is down a very substantial amount, preferably at least  
10 about 30dB down, from the far field mainlobe gain. In general, the reduced sidelobes provided by the present invention is accomplished by tapering the radiating illumination in a relatively few, precisely determined steps.

15 For purposes of further describing the invention, the more general case of a rectangular, solid state active array 60, depicted in FIGS. 3-5, is considered. Array 60 corresponds generally to array 10 (FIG. 1), insofar as general construction is concerned.

20 Also, for purposes of illustrating the invention, it may be assumed that array 60 has rectangular dimensions 2a and 2b, and has R rows and C columns of linearly polarized, rectangular radiating elements 62. Associated with element 62 is a power module 64 (shown in phantom  
25 lines).

It is, however, assumed, for purposes of simplifying the following computations, that array 60 has an elliptically (instead of a rectangular) radiating aperture 66, it having been determined by the present inventors  
30 that array corner regions 68 contribute only negligibly to sidelobes. For purposes of the following description, the far field,  $G$ , associated with radiating aperture 66 is considered, the far field at any point defined by angles  $\theta$  and  $\phi$  being generally identified as  $G(\theta, \phi)$   
35 in FIG. 3.

1        A principal feature of the present invention is  
the dividing, for analysis purposes, of radiating  
aperture 66 into a relatively few, superimposed ellip-  
tical zones around a central point "A", and the selection  
5        of zone boundary axes  $a_i$ ,  $b_i$  and the zone voltage  
amplitudes,  $E_i$ , associated therewith in a manner  
providing a tapered illumination of the aperture which  
assures very low, far field sidelobes.

10      Preferably the number of elliptical zones selected  
varies between 3 and about 10 and more preferably  
between 3 and only about 7. Insufficient illumination  
tapering is considered to be provided using less than 3  
zones and although smoother tapering can be provided by  
use of more than about 7 zones, the cost of using more  
15      than that number of different types of power modules is  
costly and has moreover, been found by the present  
inventors to be unnecessary for achieving very low  
sidelobes. For specific purposes of illustrating the  
invention, the number of zones shown and described is  
20      5; however, any limitation to the use of about 5 zones  
is neither intended nor implied.

25      First through fifth concentric, progressively larger  
elliptical zones 74, 76, 78, 80 and 82, respectively,  
are thus selected, the zones having semi-major and  
semi-minor axes equal, respectively, to  $a_1$ ,  $a_2$ ,  $a_3$ ,  
 $a_4$ , and  $a_5$  and  $b_1$ ,  $b_2$ ,  $b_3$ ,  $b_4$ , and  $b_5$  (FIG. 4).  
First zone 74 is the smallest zone and fifth zone 82 is  
the largest zone and completely fills aperture 66,  
dimensions  $a_5$  and  $b_5$  being, therefore, respectfully  
30      equal to aperture dimensions  $a$  and  $b$  (FIG. 3).

As can be seen from FIG. 5, which corresponds to  
a transverse output voltage cross-section of array 60,  
zones 74, 76, 78, 80 and 82 are, for analysis purposes,  
considered as stacked (or superimposed) upon one another,  
35      with the fifth, largest zone 82 at the bottom and the

1 first, smallest zone 74 at the top. Associated with  
each zone 74, 76, 78 and 80 and 82 is a different  
voltage amplitudes,  $E_i$ , amplitude  $E_1$  being associated  
with zone 74,  $E_2$  with zone 76,  $E_3$  with zone 78,  $E_4$   
5 with zone 80 and  $E_5$  with zone 82. In regions where  
two or more zones 74-82 overlap, the voltage amplitudes,  
 $E_i$ , are added to establish power module voltage. For  
example, in a central, elliptical region 84, defined by  
first zone 74, the combined voltage amplitude of the  
10 stacked zones 74-82 required to be provided by underlying  
power modules 60 is equal to  $E_1 + E_2 + E_3 + E_4 + E_5$ . In  
an annular region 86 of second zone 76 outside of  
first zone 74, the voltage amplitude required to be  
provided by underlying power modules 60 is equal to  
15  $E_2 + E_3 + E_4 + E_5$ ; in an annular region 88 of third  
zone 78 outside of second zone 76, the voltage amplitude  
required to be provided by the underlying power modules  
is equal to  $E_3 + E_4 + E_5$ . In turn, in an annular  
region 90 of fourth zone 80 outside of zone 78, the  
20 voltage required to be provided by underlying power  
modules 60 is  $E_4 + E_5$ ; outside of zone 80, in an  
annular region 92 of fifth zone 82, underlying power  
modules 60 are required to provide a voltages amplitude  
equal only to  $E_5$ . However, by known principles of  
25 superposition, each zone 74-82 can be treated separately  
as providing only a single, corresponding voltage  
amplitude  $E_1-E_5$ .

1        The present process treats all zone axis dimensions,  $a_i$ ,  $b_i$ , and zone voltage amplitudes,  $E_i$ , as independent variables. At least one set of values for these variables is computed which will provide, as may be required, 5 either minimum sidelobes or a sidelobe gain which is a preselected number of dB less than the corresponding mainlobe gain. These independent variables  $a_i$ ,  $b_i$  and  $E_i$  are computed, for numerous  $G(\theta, \phi)$  points, by the equation:

10        
$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \theta - \hat{a}_\phi \sin \phi \cos \theta)]^2, \quad (1)$$

wherein 
$$f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i, \quad (2)$$

$$u_i = (k_o a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi}, \quad (3)$$

15        and further wherein  $J_1(u_i)$  is the first order Bessel function,  $k_o$  is the wave number associated with the radiation and  $\hat{a}_\theta$  and  $\hat{a}_\phi$  are the unit vectors in the spherical coordinate system.

20        To determine the optimum set of parameters ( $a_i$ ,  $b_i$ ,  $E_i$ ) for low sidelobes, standard techniques of gradient search can be employed. In the optimization process an initial set of parameters is chosen as a starting point, and a present maximum sidelobe level (such as -30 dB) is selected as a performance criterion. Then the antenna far field pattern with the initial set of input parameters can be calculated by using Equation (1). Next the total power of all the sidelobes that exceed the present level, being defined as the error, is computed. After 25 this a small variation of one of the parameters, either a positive or negative increment, is introduced and the error is recomputed. By examining the trend of the error, 30 and hence the gradient (rate of change), one can decide

1 which way the following step of variation should be  
2 implemented. The process is repeated for this parameter  
3 until a local minimum in the error is obtained. By the  
4 same procedure the iteration process is carried out for  
5 all other parameters until the error is reduced to an  
6 acceptable level. This optimization process can be  
7 readily accomplished by using a computer. By way of  
8 specific example, again with no limitations being  
9 thereby intended or implied, the present inventors have  
10 determined for M equal to 5 (that is, for five aperture  
11 zones), the optimum zone boundaries,  $a_i$ ,  $b_i$ , and  
12 output voltage amplitudes,  $E_i$ . These values are shown  
13 below in Table 1, wherein  $a = a_5 = 1.3$  meters and  
14  $b = b_5 = .87$  meters, the sum of  $E_1 + E_2 + E_3 + E_4 + E_5$   
15 is normalized to 1.0 and the radiation frequency is  
16 3.25 GHz. Furthermore, for simplicity of mathematical  
17 derivation, the aspect ratio,  $b_i/a_i$ , for each zone is  
18 identical to that of each other zone.

20

TABLE 1

	$a_1$	.44 m
	$a_2$	.68 m
	$a_3$	.88 m
25	$a_4$	1.01 m
	$a_5$	1.3 m
	$b_1$	.30 m
	$b_2$	.46 m
	$b_3$	.60 m
30	$b_4$	.68 m
	$b_5$	.87 m
	$E_1$	0.26
	$E_2$	0.22
	$E_3$	0.16
35	$E_4$	0.16
	$E_5$	0.20

1 FIG. 6, directly corresponds to the righthand  
half of FIG. 5 and depicts, relatively to scale and for  
the  $b_i$  dimensions normalized to  $b = b_5 = 1$ , the corres-  
ponding, computed voltage amplitude,  $E_i$ , for each of  
5 the five zones 74, 76, 78, 80 and 82. Also shown in  
FIG. 6 is the dB value associated with the difference  
in power level across each boundary: 2.62 dB with zone  
74, 3.06 dB with zone 76, 3.1 dB with zone 78 and 5.11  
dB with zone 80.

10 For the computed  $a_i$ ,  $b_i$ ,  $E_i$  values listed in  
Table 1, there is plotted in FIG. 7 antenna pattern  
gain (in dB) against elevation angle,  $\theta$  as measured  
from the broadside axis. From FIG 7 it can be seen  
that the gains of all sidelobes 46 (shown shaded) are  
15 down at least about 36dB from the peak ( $0^\circ$ ) gain of  
mainlobe 42 over the entire visible radiation range.

20 In the foregoing, it has been assumed, for compu-  
tations involving Equation 1, that the boundaries of  
the five elliptical zones 74, 76, 78, 80 and 82 are  
perfectly elliptical, as would be the case if there  
25 were an infinite number of infinitely small power  
modules 64 distributed over antenna elements 62. In  
reality, however, each radiating zone intersects a  
finite, though usually large, number of radiating  
elements 62 so that the zone boundaries are more  
accurately approximated by a discontinuous, stepped  
shape, (FIG. 4). The question then arises as to which  
30 of two adjacent zones the intersected radiating elements  
62 (and corresponding power modules 64) should be  
allocated and also whether allocation to one zone or  
another makes any significant difference with respect  
to sidelobe gain reduction.

1        To answer this question, a specific array pattern, with actual element spacing and lattice structure taken into account, was used by the present inventors to compute aperture zone parameters  $a_i$  and  $b_i$  and voltage amplitudes,  $E_i$ . For such purposed, the actual geometric configuration of a proposed solid state radar array, having an array size of 2.6 by 1.75 meters and having 1188 rectangular radiating elements, was assumed. It was futher assumed that the zone boundaries followed actual boundries of the radiating apertures. Values of  $a_i$ ,  $b_i$  and  $E_i$  for minimum sidelobes were obtained for such an array configuration by operation of Equation 1. The computed gain VS elevation angle is plotted in FIG. 8 which shows that the highest sidelobe gain is down at least about 37 dB from the peak mainlobe gain. A comparison of FIGs. 7 and 8 thus reveals that although the sidelobe pattern is slightly different in actual conditions (FIG. 8) as compared to that of the idealized conditions (FIG. 7), the sidelobe gains are nevertheless about the same in both cases.

20       Although there has been described above apparatus and method for configuring a solid state, active array antenna aperature so as to provide about a -30 to -35dB peak sidelobe gain by using only a few different power module groups, for purposes of illustrating the manner in which the invention can be used to advantage, it is to be understood that the invention is not limited thereto. Accordingly, any and all variations and modifications which may occur to those skilled in the art are to be understood to be within the scope and spirit of the invention as defined in the appended claims.

CLAIMSWhat is claimed is:

1. A low sidelobe, solid state, phased array antenna apparatus having a far field mainlobe and sidelobe radiation pattern, the array antenna comprising:
  - 5 a) an antenna aperture formed of a large number, N, of small, closely spaced radiating apertures;
  - b) a number, equal to the number N, of linearly polarized radiating elements, each of which is operatively associated with a corresponding one of the small radiating apertures for radiating microwave energy therethrough; and
  - c) a number of solid state power modules, each of which is operatively associated with at least one of the radiating elements for providing power thereto, the number of power modules being divided into 15 a number, M, of groups of power modules, the number M being between 3 and about 10 and being much less than the number N, the output voltage amplitudes of each of the power modules being substantially the same for any group of modules and being substantially different for different groups of modules; the output voltage amplitudes of the power modules for the M different groups of modules and the boundaries of the M different groups of modules being selected so as to cause the far field sidelobe gain of the array to be down at least 20 about 30dB from the associated far field mainlobe gain of the array.

1           2. The array antenna as claimed in Claim 1  
wherein the number M is between 3 and about 7.

1           3. The array antenna as claimed in Claim 1 wherein  
the number M is about 5.

1           4. The array antenna as claimed in Claim 1  
wherein the M groups of power modules are concentrically  
arranged around a central point of the array so that  
the voltage voltage amplitudes of the power modules in  
5           each of the M different groups of modules decrease with  
increasing distance of the groups from said central  
point.

1           5. The array antenna as claimed in Claim 4  
wherein the outer boundary of each of the M groups of  
power modules is elliptically shaped, each said boundary  
having a semi-major axis of length  $a_i$  and a semi-minor  
5           axis of length  $b_i$ , wherein the subscript "i" refers to  
the ith boundary.

1           6. The array antenna as claimed in Claim 5 wherein  
the output voltage amplitudes and the arrangement of said  
M groups of power modules are selected by treating the  
M module group arrangements as comprising a superposition  
5           of M elliptically shaped, overlapping zones having the  
same boundaries as corresponding ones of the M groups  
of modules, each of said M zones having associated  
therewith a different voltage amplitude  $E_i$ , the voltage  
amplitude of the power modules in each of said M groups  
10           being selected by adding the different voltage amplitudes,  
 $E_i$ , of the corresponding overlapping zones, wherein the  
subscript "i" refers to the ith zone.

1           7. The array antenna as claimed in Claim 6  
wherein the voltage amplitudes,  $E_i$ , and semi-axis  
lengths,  $a_i$  and  $b_i$ , are selected by application of  
the following far field equation to cause the sidelobe  
5           gain to be down at least about 30dB from the mainlobe  
gain:

$$G(0, \phi) = [f(0, \phi) (\hat{a}_0 \cos \phi - \hat{a}_\phi \sin \phi \cos 0)]^2,$$

10           wherein  $f(0, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$ ,

$$u_i = (k_0 a_i \sin 0) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

15            $J_1(u_i)$  is the first order Bessel function,

20            $\hat{a}_0$  and  $\hat{a}_\phi$  are unit vectors in the spherical coordinate  
system and  $k_0$  is the wave number associated with the  
radiated field.

1           8. A low sidelobe, solid state phased array  
antenna apparatus having a far field mainlobe and sidelobe  
radiation pattern, the array antenna apparatus  
comprising:

- 5           a) an antenna aperture formed of a large number,  
 $N$ , of individual, closely spaced radiating apertures;
- 10           b) a number, equal to the number  $N$ , of  
radiating elements, each of which is operatively associated  
with a corresponding one of the radiating apertures for  
radiating microwave energy therethrough; and
- 15           c) a number of solid state power modules, each  
of which is operatively associated with at least one of  
the radiating elements for providing power thereto, the  
number of power modules being divided into a number,  $M$ ,

15 of groups of power modules, wherein the number M is  
between 3 and about 7 and is much less than the number  
N, the M groups of power modules being arranged in a  
concentric pattern around a central point of the array,  
the output voltage amplitude of each of the power  
20 modules being substantially the same in any one of the  
M groups of modules and being substantially different  
in different groups of the modules, the M groups of  
modules being arranged so that the voltage amplitudes  
of the power modules in the groups of modules decreases  
25 with increasing distance from the central point;

the output voltage amplitudes of the power  
modules in the different groups of power modules  
and the boundaries of the different groups of  
power modules being selected, in combination, to  
30 cause the far field peak sidelobe gain of the array  
to be down at least about 30 dB from the corres-  
ponding far field mainlobe gain of the array.

1 9. The array antenna as claimed in Claim 8  
wherein the outer boundary of each of the M groups of  
power modules is elliptical shaped, each said boundary  
having a semi-major axis of length  $a_i$  and a semi-minor  
5 axis of length  $b_i$  and wherein the M groups of modules  
are treated as comprising a superposition of M,  
elliptically-shaped zones having the same boundaries as  
corresponding ones of the groups of modules, each of  
the M zones having associated therewith a different  
10 voltage amplitude  $E_i$ , the voltages amplitude of the  
power modules in each of said groups of modules being  
a superposition of the different voltage amplitudes,  
 $E_i$ , of the overlapping zones associated with each of  
the groups, wherein the subscript "i" refers to the ith  
15 zone.

1           10. The array antenna as claimed in Claim 9  
wherein the amplitudes  $E_i$  and the semi-major and  
semi-minor axis lengths  $a_i$  and  $b_i$ , respectively,  
are selected by application of the following far field  
5           equation so as to cause the sidelobe gain to be down at  
least about 30dB from the mainlobe gain:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

10           wherein  $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$ ,

$$u_i = (k_o a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

15            $J_1(u_i)$  is the first order Bessel function,

20            $\hat{a}_\theta$  and  $\hat{a}_\phi$  are unit vectors in the spherical coordinate  
and  $k_o$  is the wave number associated with the radiated field.

1           11. The array antenna as claimed in Claim 8 wherein  
the number  $M$  of groups of power modules is about 5.

1           12. A process for configuring a low sidelobe  
solid state, phased array antenna, the process comprising:

- a) forming an array antenna aperture of  
a large number,  $N$ , of small, closely spaced radiating  
5           apertures;
- b) providing for each of the small radiating  
aperatures a radiating element,  $N$  radiating elements  
being thereby provided;
- c) providing for each of the radiating elements  
10           a solid state power module;

d) dividing the power modules into M different power module groups, the number M being between 3 and about 10, and being much less than the number N;

e) selecting the configuration of the M groups of power modules and the output voltage amplitude of the power modules in each of the M groups of modules so as to cause the far field peak sidelobe gain to be down at least about 30dB from the corresponding far field mainlobe gain of the array.

1 13. The process as claimed in Claim 12 wherein the number M is between about 3 and about 7.

1 14. The process as claimed in Claim 12 wherein the number M is about 5.

1 15. The process as claimed in Claim 12 including arranging the M groups of power modules concentrically around a central point of the array and so that the voltage amplitudes of the power modules in the M groups of modules 5 decreases with increasing distance from the central point.

1 16. The process as claimed in Claim 12 including arranging the M groups of power modules so that the outer boundaries thereof are substantially elliptically shaped, each boundary having a semi-major axis 5 of length  $a_i$  and a semi-minor axis of length  $b_i$ , wherein the subscript "i" refers to the  $i$ th boundary.

1           17. The process as claimed in Claim 16 including  
treating the M groups of power modules as comprising a  
superposition of M elliptically shaped, overlapping  
zones having the same boundaries as corresponding ones  
5           of the M groups of modules, each of the M zones having  
associated therewith a voltage amplitude,  $E_i$ , and  
including treating the voltage amplitude of the power  
modules in each of the M groups of power modules as an  
additive superposition of the voltages amplitudes,  $E_i$ ,  
10           of the corresponding overlapping zones, wherein the  
subscript "i" refers to the ith zone.

1           18. The process as claimed in Claim 17 including  
using the following far field equation to obtain values  
for the zone voltages amplitudes,  $E_i$ , and the zone semi-  
major and semi-minor axis lengths,  $a_i$  and  $b_i$ , which cause  
5           the far field sidelobe gain to be down at least about 30dB  
from the corresponding far field mainlobe gain:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

10           wherein  $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$ ,

$$u_i = (k_o a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

15            $J_1(u_i)$  is the first order Bessel function,

20            $\hat{a}_\theta$  and  $\hat{a}_\phi$  are unit vectors in the spherical coordinate  
and  $k_o$  is the wave number associated with the radiated field.

1           19. A process for configuring a low sidelobe,  
solid state, phased array antenna, the process comprising:

- a) providing, for an array antenna aperture, a large number,  $N$ , of small, closely spaced radiating apertures;
- 5 b) providing for each of the small radiating apertures a radiating element,  $N$  radiating elements being thereby provided;
- 10 c) providing for each of the  $N$  radiating elements a solid state power module;
- d) dividing the power modules into  $M$  different power module groups, the number  $M$  being between 3 and about 7 and being much less than the number  $N$ , the output voltage amplitude of all the power modules in 15 any of the  $M$  groups of modules being substantially the same and the output voltage amplitudes of power modules in different groups of modules being different;
- 20 e) arranging the  $M$  groups of power modules in a concentric pattern around a central point of the array so that the output voltage amplitudes of the  $M$  groups of power modules decrease with increasing distance from said central point; and
- 25 f) selecting the output voltage amplitudes of the power modules of the  $M$  groups of power modules and the boundaries of the  $M$  groups of power modules so as to cause the far field sidelobe gain of the array to be down at least about 30dB from the corresponding far field mainlobe gain of the array.

- 1 20. The process claimed in Claim 19 including arranging the  $M$  groups of power modules so that the outer boundary of each said group is substantially elliptical 5 in shape, each boundary having a semi-major axis of length  $a_i$  and a semi-minor axis of length  $b_i$  and including treating each of the  $M$  groups of power modules as a superposition of  $M$  elliptically shaped, overlapping zones having the same boundaries as corresponding ones of the  $M$  groups of power modules, each of the  $M$  zones

10 having associated therewith a voltage amplitude,  $E_i$ , and including treating the voltage amplitude of each of the  $M$  groups of modules as an additive superposition of the voltage amplitudes,  $E_i$ , of the corresponding overlapping zones, wherein the subscript "i" refers to the  $i$ th zone.

1 21. The process as claimed in Claim 20 including using the following far field equation to obtain values of zone voltage amplitudes,  $E_i$ , and of the zone semi-major and semi-minor axis lengths,  $a_i$  and  $b_i$ , which cause 5 the sidelobe gain to be down at least about 30dB from the mainlobe gain:

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

10 wherein  $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$ ,

$$u_i = (k_o a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

15  $J_1(u_i)$  is the first order Bessel function,  
 $\hat{a}_\theta$  and  $\hat{a}_\phi$  are unit vectors in the spherical coordinate and  $k_o$  is the wave number associated with the radiated field.

1 22. A process for configuring a low sidelobe, solid state phased array antenna, the process comprising:

a) providing, for an array antenna aperture, a large number,  $N$ , of small, closely spaced radiating 5 apertures;

b) providing for each of the  $N$  small radiating apertures a radiating element and a solid state power module, a number  $N$  of radiating elements and  $N$  power modules being thereby provided;

10                   c) dividing the array antenna aperture into a number,  $M$ , of differently sized, overlapping concentric zones of elliptical shape, each of said zones having a semi-major axis of length,  $a_i$ , and a semi-minor axis of length,  $b_i$ ;

15                   d) selecting, by use of the following far field equation, values of  $E_i$ ,  $a_i$  and  $b_i$  which cause the far field sidelobe gain of the array to be down by at least about 30dB from the corresponding far field mainlobe gain;

20

$$G(\theta, \phi) = [f(\theta, \phi) (\hat{a}_\theta \cos \phi - \hat{a}_\phi \sin \phi \cos \theta)]^2,$$

25                   wherein  $f(\theta, \phi) = \sum_{i=1}^M 2\pi a_i b_i E_i J_1(u_i)/u_i$ ,

$$u_i = (k_0 a_i \sin \theta) \sqrt{\cos^2 \phi + (b_i^2/a_i^2) \sin^2 \phi},$$

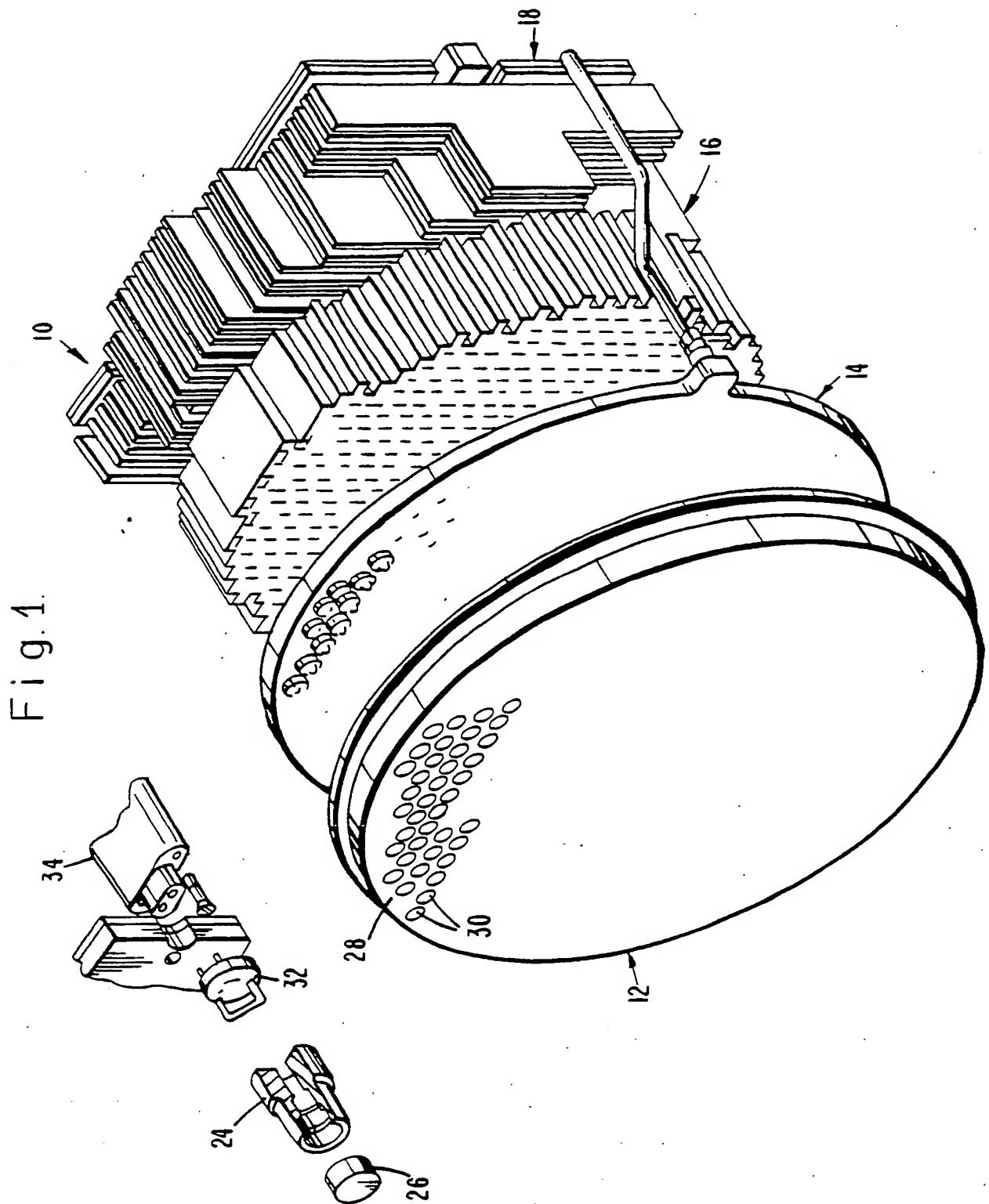
30                    $J_1(u_i)$  is the first order Bessel function;

$\hat{a}_\theta$  and  $\hat{a}_\phi$  are unit vectors in the spherical coordinate,  $k_0$  is the wave number associated with the radiated field and the subscript "i" refers to the  $i$ th zone;

35                   e) combining the  $E_i$  values for overlapping areas of said zones and selecting the output voltages amplitudes of power modules underlying the overlapped zones to be equal to said combined  $E_i$  values.

1                   23. The process as claimed in Claim 22 wherein the number  $M$  is between 3 and about 10.

1                   24. The process as claimed in Claim 22 wherein the number  $M$  is about 5.



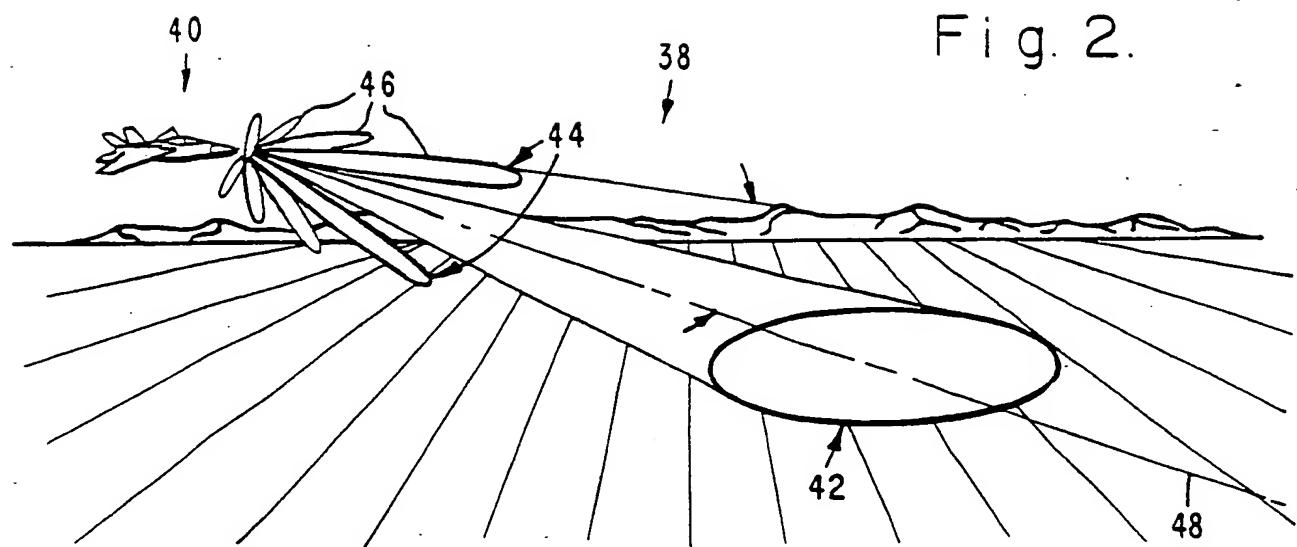
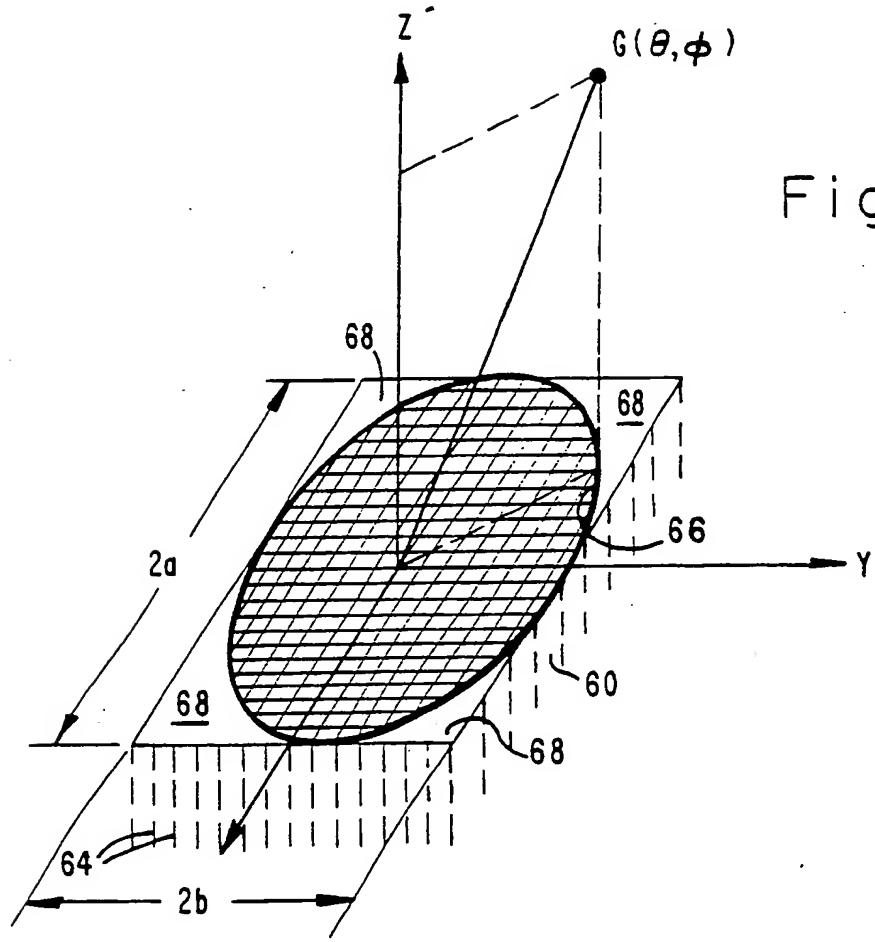


Fig. 3.



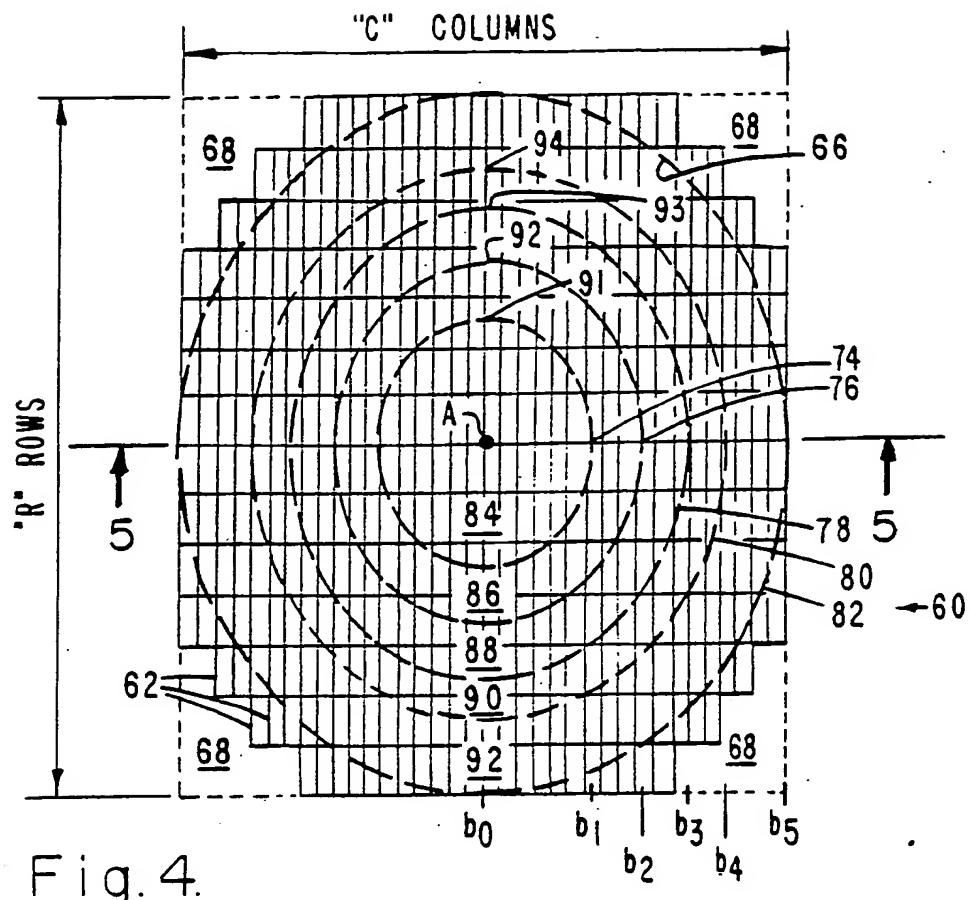
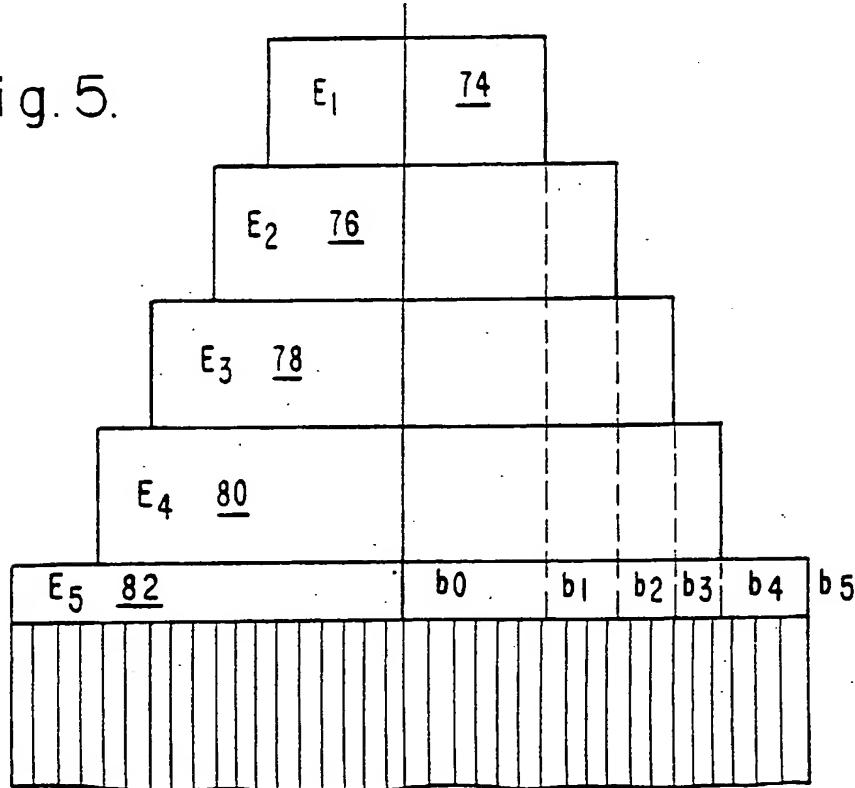


Fig. 4.

Fig. 5.



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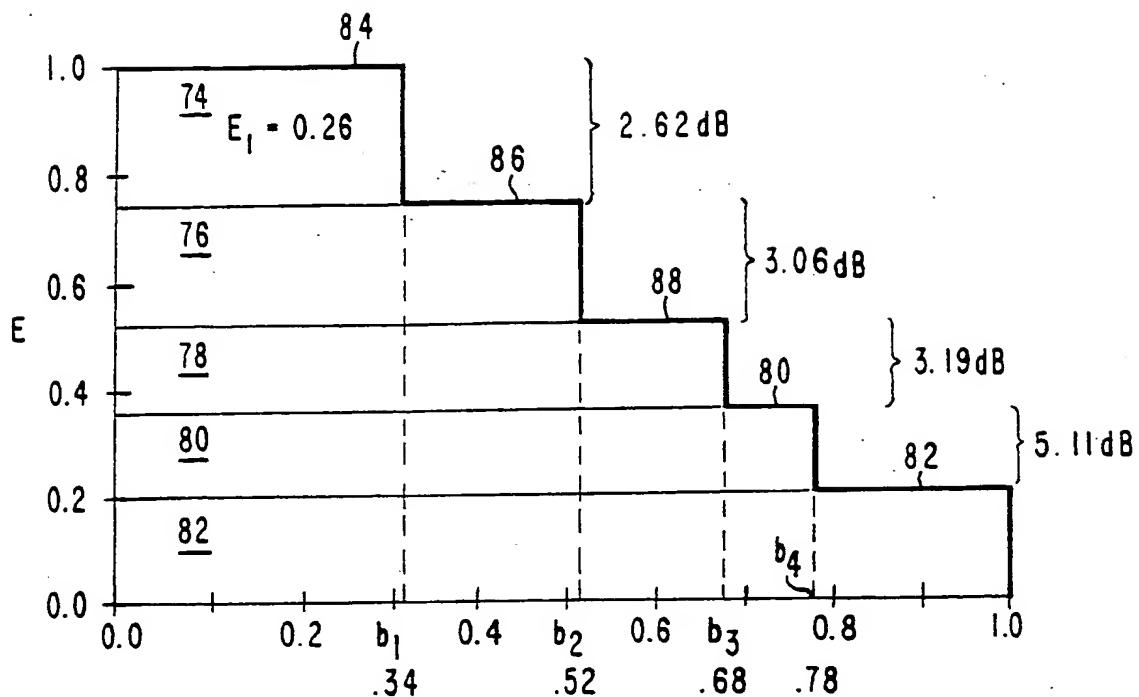
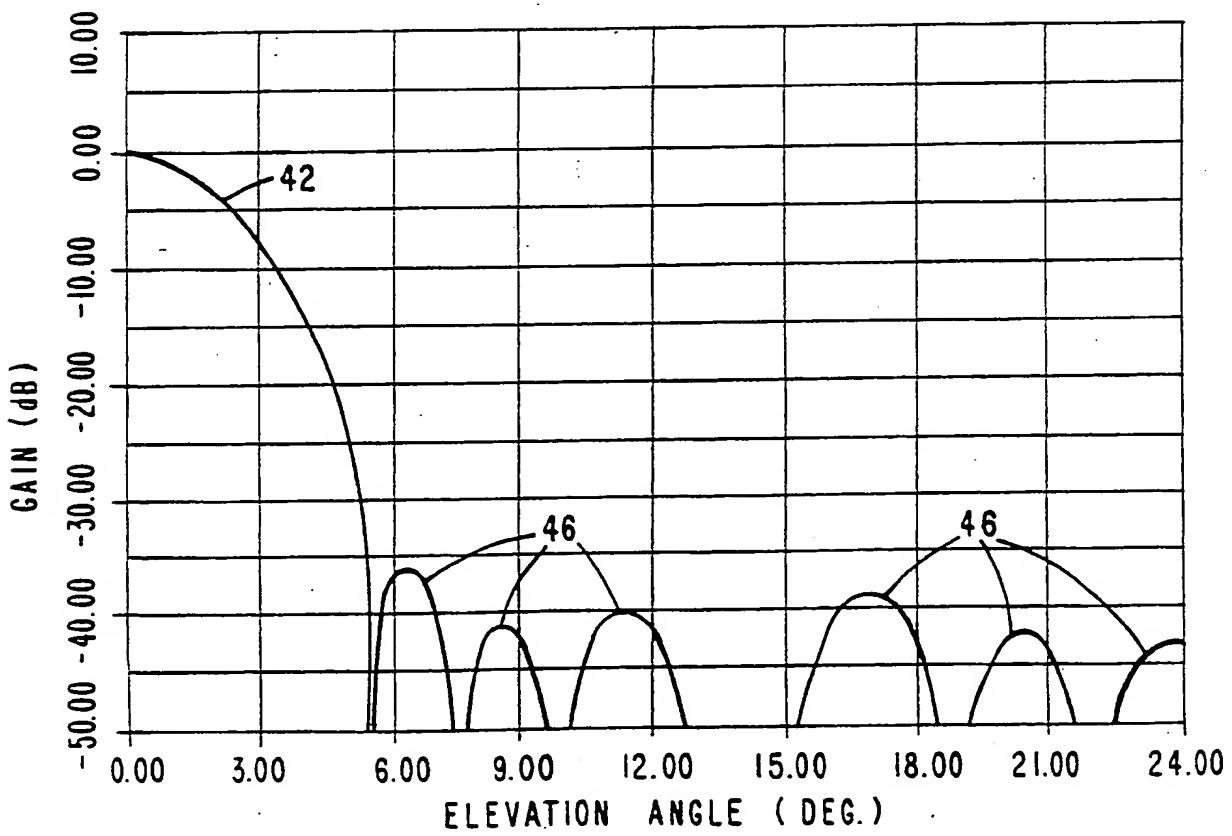


Fig. 6.

Fig. 7.



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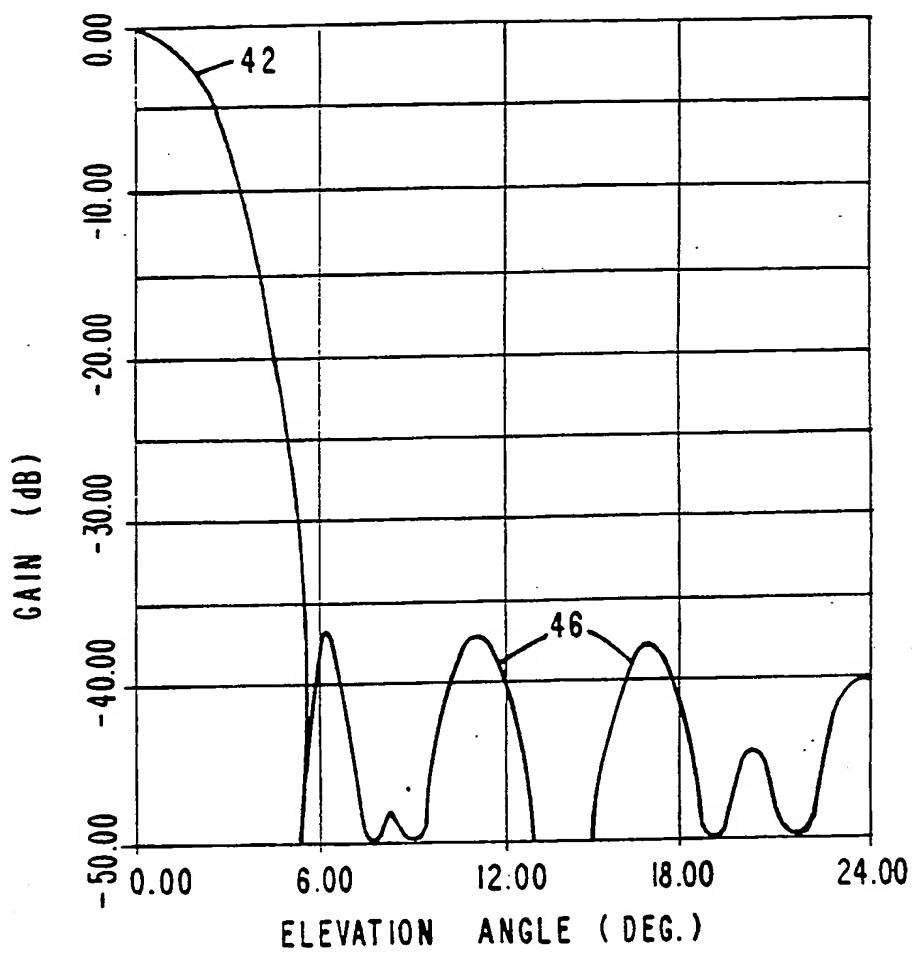


Fig. 8.

# INTERNATIONAL SEARCH REPORT

International Application No. PCT/US 87/01755

## I. CLASSIFICATION OF SUBJECT MATTER (if several classification symbols apply, indicate all) <sup>6</sup>

According to International Patent Classification (IPC) or to both National Classification and IPC

IPC<sup>4</sup> : H 01 Q 21/22; H Q1 Q 21/00

## II. FIELDS SEARCHED

Minimum Documentation Searched <sup>7</sup>

Classification System	Classification Symbols
IPC <sup>4</sup>	H 01 Q

Documentation Searched other than Minimum Documentation  
to the Extent that such Documents are Included in the Fields Searched <sup>8</sup>

## III. DOCUMENTS CONSIDERED TO BE RELEVANT<sup>9</sup>

Category <sup>10</sup>	Citation of Document, <sup>11</sup> with indication, where appropriate, of the relevant passages <sup>12</sup>	Relevant to Claim No. <sup>13</sup>
Y	1982 IEEE MTT-S International Microwave Symposium Digest, 15-17 June 1982, Dallas, Texas, IEEE (New York, US), D.N. McQuiddy, Jr: "Solid state radar's path to GaAs", pages 176-178 see pages 176-177, left-hand column with figures 1-3 --	1-4,8,12-15,19
Y	US, A, 3760345 (HUGHES) 18-September 1973 see column 1, lines 35-54; column 2, line 30 - column 5, line 38 with figures 1-5 --	1-4,8,12-15,19
A	IEEE Transactions on Antennas and Propagation, volume AP-33, no. 8, August 1985, IEEE, (New York, US), R.L. Haupt: "Reducing grating lobes due to subarray amplitude tapering", pages 846-850 see pages 846,849, sections I and II --	1-4,8,12-15,19 --

\* Special categories of cited documents: <sup>10</sup>

"A" document defining the general state of the art which is not considered to be of particular relevance

"E" earlier document but published on or after the international filing date

"L" document which may throw doubts on priority, claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)

"O" document referring to an oral disclosure, use, exhibition or other means

"P" document published prior to the international filing date but later than the priority date claimed

"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention

"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step

"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art.

"&" document member of the same patent family

## IV. CERTIFICATION

Date of the Actual Completion of the International Search

3rd November 1987

Date of Mailing of this International Search Report

- 1 DEC 1987

International Searching Authority

EUROPEAN PATENT OFFICE

Signature of Authorized Officer

M. VAN MOL

## III. DOCUMENTS CONSIDERED TO BE RELEVANT (CONTINUED FROM THE SECOND SHEET)

Category	Citation of Document, with indication, where appropriate, of the relevant passages	Relevant to Claim No
A	US, A, 3553706 (CHARLTON) 5 January 1971 see column 1, lines 11-23; figures 1a-c and 5 --	1,5-12, 16-19,22- 24
A	US, A, 3811129 (HOLST) 14 May 1974 see abstract; column 6, lines 10-36 --	1-4,8,12- 15,19,22
A	US, A, 4052723 (MILLER) 4 October 1977 see abstract and figures 2-5 -----	1,8,12 19,22

ANNEX TO THE INTERNATIONAL SEARCH REPORT ON

INTERNATIONAL APPLICATION NO.

PCT/US 87/01755 (SA 18210)

This Annex lists the patent family members relating to the patent documents cited in the above-mentioned international search report. The members are as contained in the European Patent Office EDP file on 12/11/87

The European Patent Office is in no way liable for these particulars which are merely given for the purpose of information.

Patent document cited in search report	Publication date	Patent family member(s)	Publicat date
US-A- 3760345	18/09/73	None	
US-A- 3553706	05/01/71	None	
US-A- 3811129	14/05/74	None	
US-A- 4052723	04/10/77	None	